## Mathematics Assessment Program $C \mathbf{C R}-\boldsymbol{B} 2$

## College and Career Readiness Mathematics

Time allowed: 90 minutes
These tasks give you a chance to show what you know and how you reason, and to solve mathematical problems.

Please show your work and reasoning in the spaces provided. Explain any assumptions you make.

Try as many tasks as you can in the time given. If you get stuck on a task, move on to the next task.

Name: $\qquad$ Male Female

School: $\qquad$ City: $\qquad$
Teacher: $\qquad$ Grade: $\qquad$
Date: $\qquad$

Do not write in the box below:

| CCR-B2 | Short <br> Tasks | T-shirt <br> Sale | Glasses | Table <br> Tiling | Temple <br> Geometry | Cross <br> Totals | Total |
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These tests were developed with support from the Bill and Melinda Gates Foundation

## Short Tasks

1. Simplify $(\sqrt{ } 2-\sqrt{ } 3)^{2}$
2. If $x$ is positive and $x \neq 1$, simplify $\frac{\sqrt{x}}{x^{3}}$.
3. Jane, Maria, and Ben each have a collection of marbles. Jane has 15 more marbles than Ben, and Maria has 2 times as many marbles as Ben. All together they have 95 marbles.
Find how many marbles Maria has.
4. If $x$ and $y$ are integers and $x+y<11$, and $x>6$.

What is the smallest possible value of $x-y$ ?
5. This graph shows the journey of a motorbike and a car.

Find the distance between the motorbike and the car at $\mathrm{t}=0, \quad 1, \quad 2, \quad 3, \quad 4, \quad 5$ seconds.

Sketch a graph of the separation over time.


## T-shirt Sale

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## Any 3 T-shirts for $\mathbf{\$ 1 4 . 5 0}$



1. Tom bought these three T-shirts at the sale price of $\$ 14.50$.

How much money did he save compared to the original total price of the T-shirts?
Show your calculations.
\$ $\qquad$
2. What percentage of the original total price did Tom save? $\qquad$ \%

Show your work.
3. Harry also paid $\$ 14.50$ for three T-shirts at the sale. The sale price saved Harry $30 \%$ of the original price of the three T-shirts.
What is the original total price of his three T-shirts?
\$ $\qquad$
Show your calculations.

## Glasses

This diagram shows three glasses (not drawn to scale).
The measurements are all in centimeters.

| The volume of a cylinder $=\pi r^{2} h$ |
| :---: |
| The volume of a sphere $=\frac{4 \pi r^{3}}{3}$ |
| The volume of a cone $=\frac{\pi r^{2} h}{3}$ |



The bowl of glass 1 is cylindrical. The diameter is 5 cm and the height is 6 cm .
The bowl of glass 2 is a cylinder with a hemispherical bottom. The diameter is 6 cm and the height of the cylinder is 3 cm .

The bowl of glass 3 is an inverted cone. The diameter is 6 cm and the slant height is 6 cm .

1. Find the vertical height of the bowl of glass 3 . Show your work.
$\qquad$ cm.
2. Calculate the volume of the bowl of each of these glasses. Show your work.
a. Glass 1
$\qquad$ $\mathrm{cm}^{3}$
b. Glass 2
$\qquad$ $\mathrm{cm}^{3}$
c. Glass 3
$\qquad$ $\mathrm{cm}^{3}$
3. Find the height of liquid in Glass 2 when it is half full. Show your calculations.


Please show your work on the page opposite.

Table Tiling (continued)
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During the Edo period (1603-1867) of Japanese history, geometrical puzzles were hung in the holy temples as offerings to the gods and as challenges to worshippers.

This is one such problem.
Inside a large circle with radius 2 r , two circles of radius $r$ are drawn.

Four smaller circles, of radius $p$, are drawn to touch the large circle and the circles of radius $r$.

The following questions will help you to find the relationship between $r$ and $p$


1. In the right triangle DOB , explain why the length of OD is $2 \mathrm{r}-\mathrm{p}$
$\qquad$
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$\qquad$
2. Use the Pythagorean theorem in triangle DOB to find an expression for $\mathrm{OB}^{2}$.
3. In the right triangle $A D E$, explain why the length of $A E$ is $r-p$.
4. Use the Pythagorean theorem in triangle ADE to find an expression for $\mathrm{ED}^{2}$.
5. Use your results from questions 2 and 4 , and the fact that $O B=E D$ to show that $r=2 p$
6. Show that the shaded area of the diagram has area $\pi r^{2}$.

## Cross Totals

Crosses follow two rules:

- They must contain all the numbers from 1 to 9
- The horizontal and vertical totals must be equal. (We call this the Cross Total).

In the cross shown here, the Cross Total is 27 because:
adding horizontally:
adding vertically:
$2+1+9+8+7=27$
$6+4+9+3+5=27$
Which Cross Totals are possible?
Which are impossible?
Prove that you are correct.

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