## Mathematics Assessment Program <br> CCR-A1

## College and Career Readiness Mathematics

Time allowed: 40 minutes
These tasks give you a chance to show what you know and how you reason, and to solve mathematical problems.

Please show your work and reasoning in the spaces provided. Explain any assumptions you make.

Try as many tasks as you can in the time given. If you get stuck on a task, move on to the next task.

Name: $\qquad$ Male Female

School: $\qquad$ City: $\qquad$
Teacher: $\qquad$ Grade: $\qquad$
Date: $\qquad$

Do not write in the box below:

| CCR-A1 | Short Tasks | Sale! | Functions | Proofs of the <br> Pythagorean <br> Theorem | Total |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 11 |  |  |  |  |  |

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## Short Tasks

1. Simplify $(3 \sqrt{ } 5-2 \sqrt{ } 3)(3 \sqrt{ } 5+2 \sqrt{ } 3)$
2. Identify the zeros of $\mathrm{f}(\mathrm{x})=-x^{2}-3 x+4=-(x+4)(x-1)$.
$\qquad$
Sketch a rough graph of $f(x)$.

3. If $x^{2}-y^{2}=55$, and $x-y=11$, find the value of $y$.
4. These three graphs show the functions $y=x^{2} \cdot y=x^{2}+3 \cdot y=3 x^{2}$. Label the three graphs.

5. Find the equation of a circle with centre $(2,1)$ radius 5 .

## Sale!

The following price reductions are available.
Two for the price of one
Buy one and get $\mathbf{2 5 \%}$ off the second

Buy two and get $\mathbf{5 0 \%}$ off the second one
Three for the price of two

1. Which of these four different offers gives the biggest price reduction?
$\qquad$
Explain your reasoning clearly
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
2. Which of these four different offers gives the smallest price reduction?

Explain your reasoning clearly.
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$\qquad$
$\qquad$

## Functions

On the grid are eight points from two different functions.
A certain linear function passes through exactly four of the points shown.
A certain quadratic function passes through the remaining four points.
For the linear function:
1.Write the coordinate pairs of its four points.
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$\qquad$
$\qquad$
$\qquad$

Draw the line on the grid.

2.Write an equation for the function.

Show your work.

For the quadratic function:
3. Write the coordinate pairs of its four points.

Draw the graph of the function on the grid.
4. Write an equation that fits the quadratic function. Show your work.

## Proofs Of The Pythagorean Theorem?

Here are three attempts to prove the Pythagorean theorem.
Look carefully at each attempt. Which is the best 'proof' ?
Explain your reasoning as fully as possible.

## Attempt 1:

Suppose a right triangle has sides of length
$a, b$ and $c$
Draw squares on the three sides as shown.
Divide these squares into smaller squares.
You can see that the number of squares on the two shorter sides add up to make the number of squares on the longest side.
So: $a^{2}+b^{2}=c^{2}$


## Attempt 2

Suppose that you start with four right triangles with sides of length $a, b$ and $c$ and a square tray with sides of length $a+b$.

$a+b$
 one large square hole. This
 has an area of $c^{2}$.
Since these areas are equal
$a^{2}+b^{2}=c^{2}$

## Attempt 3:

The proof of the Pythagorean theorem is clear from this diagram.
The squares on the two shorter sides of the black triangle are each made from two congruent triangles.
These fit together to make the square on the longest side- the hypotenuse.


The best proof is attempt number
This is because:
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$\qquad$

My criticisms of the other proofs are:
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$\qquad$
$\qquad$
$\qquad$

